## Stability of structures

## Home exercises 5 and 6

Home exercise 5. Determine the maximum defection and maximum moments at supports and in span as a function of the compressive force P for the beam shown below.



Home exercise 6. Determine the critical buckling moment in the form  $M_{\rm cr} = \lambda \sqrt{EI_y GI_t}/L$ , where the parameter  $\lambda = \lambda(k, h/L)$ . Draw the critical load parameter  $\lambda$  as a function of k, when  $k \in (-1, 1)$  and  $L/h = 20, \nu = 0$ . Use the principle of minimum potential energy or some other numerical method and use trigonometric trial functions.



The expression for the total potential energy is

$$\Pi = \frac{1}{2} \int_{0}^{L} \left[ GI_t(\varphi')^2 + EI_y(w'')^2 + 2(M_z^0 \varphi)'w' \right] dx$$
$$= \frac{1}{2} \int_{0}^{L} \left[ GI_t(\varphi')^2 + EI_y(w'')^2 + 2(M_z^0'\varphi + \varphi'M_z^0)w' \right] dx$$